

8-3

Solving Quadratics

Objective: I can solve quadratic equations by factoring and using the zero-product property.

I can write a quadratic equation given the zeros or x-intercepts

Vocabulary: Zeros/Roots, X-Intercepts, Zero-Product Property, Solve,

What does it mean to "solve" an equation?

$$x = 5$$

The Zero-Product Property

$$(\text{?})(\text{??})=0$$

The Zero-Product Property

If $ab = 0$, then $a = 0$ or $b = 0$ or both a and b are 0

Solve

$$(x + 5)(2x - 3) = 0$$

$$x + 5 = 0$$

$$\quad -5 \quad -5$$

$$x = -5$$

Your turn! Solve

$$(x - 1)(4x + 7) = 0$$

$$x - 1 = 0$$

$$\quad +1 \quad +1$$

$$x = 1$$

$$4x + 7 = 0$$

$$\quad -7 \quad -7$$

$$\frac{4x}{4} = \frac{-7}{4}$$

$$x = -\frac{7}{4}$$

Solve

$$x(x + 9) = 0$$

$$x = 0$$

$$x + 9 = 0$$

$$\quad -9 \quad -9$$

$$x = -9$$

Solve by factoring

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$$x^2 + 5x + 4 = 0$$

$$(x+4)(x+1) = 0$$

$$x+4=0$$

$$x+1=0$$

$$x = -4, -1$$

$$2x^2 + 12x = -18$$

$$18 + 18$$

$$2x^2 + 12x + 18 = 0$$

Solve by factoring

$$x^2 + 10x + 15 = -6$$

$$x^2 - 5x + 4 = 4$$

The length of a rectangle is 8 feet more than its width. If the area of the rectangle is 84 square feet, what are the dimensions of the rectangle?

Try to solve by factoring...

$$x^2 - 2x - 24 = 0$$

What now?!

Quadratic Formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$ax^2 + bx + c$$

Solve using the quadratic formula

$$\underbrace{3a^2}_{a} \underbrace{-6a}_{b} \underbrace{-34}_{c} = 0 \quad \frac{6 \pm \sqrt{(-6)^2 - 4(3)(-34)}}{2(3)}$$

$$4n^2 + 11n = 15$$

$$\frac{6 \pm \sqrt{36 + 408}}{6}$$

$$x = 9.5, 2.5$$