

4-3 Solving Exponential and Logarithmic equations

Objectives:

I can solve exponential and logarithmic equations both graphically and algebraically.

$$\log_4 \cancel{4}^{2x} = \log_4 256$$

$$2x = \log_4 256$$

$$\frac{2x}{2} = \frac{4}{2}$$

$$x = 2$$

$$\cancel{\log_4} 4^{2x} \log_4 250$$

$$2x = \log_4 250$$

$$\frac{2x}{2} = \frac{3.98}{2} \dots$$

$$x = 1.99 \dots$$

$$\cancel{\log_e} e^{(x-1)} = 5$$

$$x-1 = \ln 5$$

$$x = 1.6$$

$$\frac{10}{5} = \frac{5e^{4x}}{5}$$

$$\ln 2 = \ln e^{4x}$$

$$\ln 2 = 4x$$

$$\frac{.69}{4} = \frac{4x}{4}$$

$$x = .17$$

$$5^{x-1} - 4 = 7$$

$$+4 \quad +4$$

$$\log_5 5^{x-1}$$

$$\equiv \log_5 11$$

$$\ln x = 4$$

$$e^4 = x$$

$$10.6 = x$$

$$\frac{2 \ln(x + 1)}{2} = \frac{4}{2}$$

$$\ln(x + 1) = 2$$

$$e^2 = x + 1$$

$$x =$$

$$\log_3(2x - 4) = 4$$

$$3^4 = 2x - 4$$

$$\begin{array}{r} 81 = 2x - 4 \\ +4 \quad \quad +4 \end{array}$$

$$\frac{85}{2} = \frac{2x}{2} \quad x = 42.5$$

$$\log_3 \cancel{6}^{3x} = 12 \quad \log_3 x = .462$$

Solve the following

$$\log(4x) = 2$$

$$4 \ln(x + 7) - 5 = 1$$

Your house cost \$250,000 and appreciates at a rate of 3% every year. How long will it take to reach \$300,000?

$$\frac{250,000(1+0.03)^x}{250,000} = \frac{300,000}{250,000}$$

$$\log_{1.03}(1.03)^x = \log_{1.03} 1.2$$
$$x = 6.16$$